

## MATHEMATICS 30 – Special Topics in Mathematics – Syllabus (Spring, 1987)

**Topic:** Combinatorial and Discrete Mathematics

**Text:** Discrete and Combinatorial Mathematics, an Applied Approach, by Ralph P. Grimaldi, Addison-Wesley, 1985.

**Course Outline** (based on text above)

**1. Basic counting techniques – 2 weeks – chap. 1**

Rules of sum and product, permutations  
Combinations  
Combinations with repetition

**2. The language of logic and set theory , 1- ½ weeks – Chap. 2 Sect. 1-4**

Propositional calculus and truth tables – lightly  
Sets, set operations, set theoretic identities

**3. Relations and functions and their uses in counting – 3 weeks – Chap.3, Chap. 5, Sect. 1-3**

Functions

Injections, surjections, counting these, Stirling numbers of 2<sup>nd</sup> kind Pigeonhole principle  
Composition, bijection, inverses

Relations

Properties, examples  
Partial orders  
Directed graphs – introduction

**4. Inclusion and Exclusion – 1 week – Chap. 7 Sect. 1-3**

Basic principles and examples (Omit Euler  $\phi$ -function), Stirling numbers again  
Derangements

**5. Generating functions – 2 weeks – Chap. 10 Sect. 1-4**

Definitions and examples  
General binomial coefficient,  $nCr$  for  $n \in \mathbb{R}$   
Partitions and Ferrers diagrams  
Exponential generating functions

**6. Graphs – 3 weeks – Sect. 5.2 again, Chap. 14 Sect. 1-4, optional 14.5, 14.6**

Introduction and examples

Subgraphs, complements, isomorphism

Vertex degree and Euler paths and cycles

Planar graphs: statement of Kuratowski's theorem

Optional: Hamilton paths and cycles

Graph coloring, chromatic polynomials

Total 12-1/2 weeks

1-1/2 weeks – exams and review