## Mathematics Department Brooklyn College, City University of New York Math 3202 (Mathematical Modeling and Simulation) 4 hours, 4 credits

Suggested Textbooks:

- A First Course in Mathematical Modeling, 5th ed, by Giordano, Fox and Worton, Brooks/Cole Publication, 2014

- Mathematical Modeling: A Case Studies Approach, by Illner, Bohun, McCollum, Roode, STML 27, American Mathematical Society, 2005

- Simulation, 5th Edition, by Sheldon Ross, Academic Press, 2012.

- 1. Discrete-time deterministic models
  - Modeling change with one-dimensional difference equations
  - Approximating change with one-dimensional difference equations
  - Exact solutions to linear difference equations; existence and stability of equilibria
  - Systems of difference equations; existence and stability of equilibria
  - Numerical simulation of difference equations: regular vs chaotic behavior

## 2. Discrete-time probabilistic models

- Random numbers generation
- Monte Carlo simulation and deterministic problems
- Monte Carlo simulation and probabilistic problems
- Inventory models
- Queuing models
- Markov chains with a finite state space; connection with difference equations models
- 3. Continuous-time deterministic models
  - Modeling change with a differential equation
  - Graphical solutions of autonomous first-order differential equations; qualitative theory
  - Numerical simulation of one-dimensional differential equations: Euler's method
  - Graphical solutions of systems of autonomous first-order differential equations
  - Euler's method for systems of differential equations
  - Chaotic behavior: the Lorenz attractor
- 4. Continuous-time probabilistic models
  - Methods to generate normal random variables
  - Methods to generate Poisson and exponential random variables
  - Poisson process
  - Brownian motion
  - Stochastic differential equations and the Euler-Maruyama method