# Mathematics Department <u>Brooklyn College, City University of New York</u> Math 3601 (Investment Science) Syllabus 4 hours, 4 credits

#### **Introduction**

Cash flows, comparison principle, arbitrage, typical investment problems (pricing and hedging)

## **Basic Theory of Interest**

Simple and compound interest, net present value, internal rate of return, evaluation of investment projects, cash cycle problems

## **Fixed income securities**

Valuation of annuities(perpetual and finite-life), annual worth, amortization, bond pricing, yield rate, price-yield curve, Macaulay duration, modified duration, duration of a portfolio.

## Term structure of interest rates and applied interest rate analysis

The yield curve, spot rate, forward rate, short rate, expectation dynamics, spot rate forecasts, invariance theorem, running present value, Fisher-Weil duration, Quasi-modified duration, capital budgeting, cash matching, running dynamic programming, Harmony theorem.

## Mean-variance portfolio theory and Capital Asset Pricing Model(CAPM)

Review of basic probability, Portfolio mean and variance, minimum variance set, efficient frontier, the Markowitz model, two-fund theorem, one-fund theorem, capital market line, beta of a portfolio, security market line, CAPM as a pricing formula, arbitrage pricing theory.

#### **Introduction to derivative securities**

Forwards, futures and swaps, binomial lattice model, random walks, Wiener process, stock price process, Ito's lemma, option concepts(call and put options), put-call parity, binomial option pricing theory, risk-neutral pricing, Black-Scholes equation, Black-Scholes formula. Greeks, volatility smile.

#### **Other topics**

Value at risk and its computations, conditional value at risk, other risk measures.