# Mathematics Department <u>Brooklyn College, City University of New York</u> Math 3802 (Introduction to Risk Theory) Syllabus 4 hours, 4 credits

## Utility Theory in Insurance

Classes of utility functions The expected utility model

## Individual Risk Model

Mixed distributions and risks Convolutions and Transforms of cumulative distribution functions Approximations: Central Limit Theorem, Translated gamma and Normal power

### **Collective Risk Models**

Compound distributions Convolution formula for a compound cumulative distribution function Distributions for the number of claims Properties of compound Poisson distributions Panjer's recursion Compound distributions and the Fast Fourier Transform Approximations for compound distributions Comparison between individual and collective risk model

## Loss Distributions

Review: techniques to generate pseudo-random samples and maximum likelihood estimates Poisson and Negative Binomial claim number distribution Gamma, Inverse Gaussian, Exponential, Lognormal and Pareto claim severity distributions

#### Ruin Theory

The classical ruin process Lundberg's inequality Ruin probability and capital at ruin Explicit expressions for ruin probabilities: the case of exponential distributions Approximation of ruin probabilities

#### Premium Principles and Risk Measures

Examples of premium principles and their properties Characterizations of premium principles Premium reduction by coinsurance Value-at-Risk and related risk measures

## **Reinsurance**

Stop-loss reinsurance Proportional reinsurance